

Ch-3 Linear Equation in Two Variables

An equation of the form $ax+by+c=0$ where a, b and c are real numbers and $x \neq y$ are variables is called linear equation in two variables.

$$[a \neq 0, b \neq 0]$$

General Form $\rightarrow a_1x + b_1y + c_1 = 0$

$$a_2x + b_2y + c_2 = 0$$

Eg:- $9x + 3y = 12$ — ①

$18x + 6y = 24$ — ②

Relationship between coefficients	Graph	No. of Solutions	Consistency of system
$a_1/a_2 \neq b_1/b_2$	Intersecting lines	Unique sol.	consistent
$a_1/a_2 = b_1/b_2 \neq c_1/c_2$	Parallel lines	No sol.	inconsistent
$a_1/a_2 = b_1/b_2 = c_1/c_2$	Coincident lines	Infinite sol.	consistent

Consistent system:- A system of linear equations is said to be consistent if it has at least one solution.

Inconsistent system:- A system of linear equation is said to be inconsistent if it has no solutions.

Ex 3.1

Q1. Aftab tells his daughter "Seven years ago, I was seven times as old as you were then. Also, three years from now, I shall be three times as old as you will be." Represent this situation algebraically and graphically.

Case I: (7 years ago)

$$\text{Aftab age} = (x - 7) \text{ years}$$

$$\text{Daughter's age} = (y - 7) \text{ years}$$

$$\text{Aftab age} = 7 (\text{daughter age})$$

$$x - 7 = 7(y - 7)$$

$$x - 7 = 7y - 49$$

$$x - 7y = -49 + 7$$

$$x - 7y = -42$$

Present ages

$$\text{Aftab} = x$$

$$\text{Daughter} = y$$

Case II (after 3 years)

$$\text{Aftab age} = (x + 3) \text{ years}$$

$$\text{Daughter's age} = (y + 3) \text{ years}$$

$$\text{Aftab age} = 3 (\text{daughter's age})$$

$$x + 3 = 3(y + 3)$$

$$x + 3 = 3y + 9$$

$$x - 3y = 9 - 3$$

$$x - 3y = 6$$

82. The coach of a cricket team buys 3 bats and 6 balls for ₹3900. Later, she buys another bat and 3 more balls of the same kind for ₹1300. Represent this situation algebraically and ~~graphically~~ geometrically.

Case I $3x + 6y = 3900$

$$3(x + 2y) = 3900$$

$$x + 2y = \frac{3900}{3}$$

$$x + 2y = 1300 \quad \text{--- (1)}$$

$$\text{bat} = x$$

$$\text{ball} = y$$

Case II

$$x + 3y = 1300 \quad \text{--- (2)}$$

~~Graph~~

3. The cost of 2kg of apples and 1kg of grapes one day was found to be ₹160. After a month, the cost of 4kg of apples and 2kg of grapes is ₹300. Represent the situation algebraically.

Case I $2x + y = 160$

$$\text{apple} = x$$

$$\text{grapes} = y$$

Case II

$$4x + 2y = 300$$

$$2(2x + y) = 300$$

$$2x + y = \frac{300}{2}$$

$$2x + y = 150$$

Ex 3.2

1. Form the pair of linear equations in the following problems, and find their solutions graphically

i) 10 students of class X took part in a Math quiz. If the no. of girls is 4 more than the no. of boys, find the no. of boys and girls who took part in the quiz.

No. of girls = y

No. of boys = x

Case I Total no. of students

$$x + y = 10 \quad - (1)$$

Case II no. of girls = 4 more than boys

$$y = 4 + x \quad - (2)$$

$$x + y = 10 \quad - (1)$$

$$y = 4 + x \quad - (2)$$

$$\Rightarrow x + y = 10$$

$$x + 4 + x = 10$$

$$x = 10 - 4$$

$$\underline{x = 6}$$

x	6	5
y	4	5

$$\Rightarrow x + 5 = 10$$

$$x = 10 - 5$$

$$\underline{x = 5}$$

$$\Rightarrow y = 4 + x \quad - (2)$$

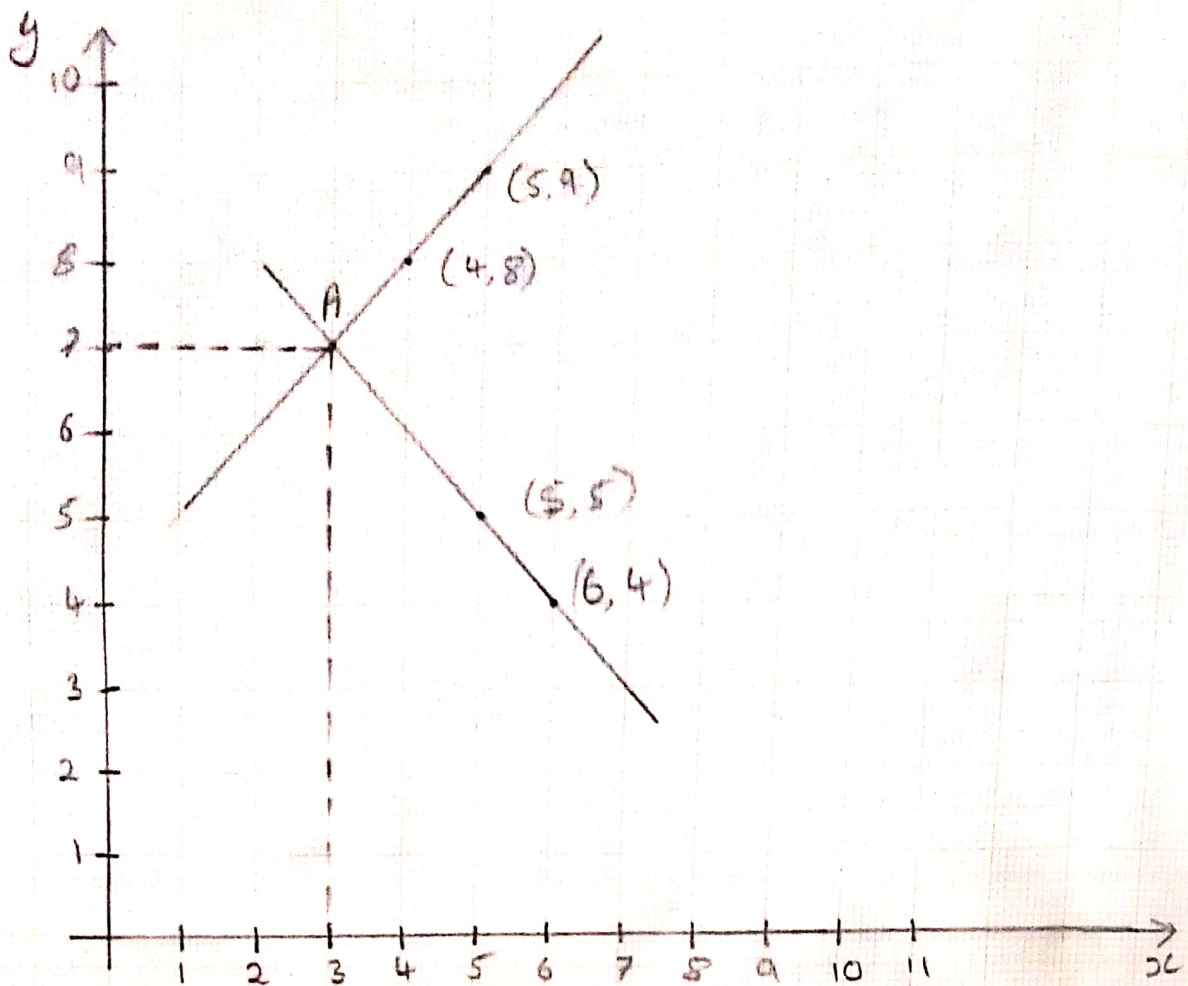
$$y = 4 + 4$$

$$\underline{y = 8}$$

x	4	5
y	8	9

$$\Rightarrow y = 4 + 5$$

$$\underline{y = 9}$$



Two lines meet at A

A (3, 7)

$$\therefore x = 3$$

$$y = 7$$

no. of boys = 3, no. of girls = 7

ii) 5 pencils and 7 pens together cost ₹ 50, whereas 7 pencils and 5 pens together cost ₹ 46. Find the cost of one pencil and one pen.

Let cost of one pencil = Rs x

Cost of one pen = Rs y

Case I $5x + 7y = 50$ — (1)

Case II $7x + 5y = 46$ — (2)

$$\Rightarrow 5x + 7y = 50 \text{ — (1)}$$

$$7y = 50 - 5x$$

$$y = \frac{50 - 5x}{7}$$

$$y = \frac{50 - 5(3)}{7} = \frac{50 - 15}{7} = \frac{35}{7} = 5$$

x	3	10
y	5	0

$$y = \frac{50 - 5x}{7} = \frac{50 - 5(10)}{7} = \frac{50 - 50}{7} = \frac{0}{7} = 0$$

$$\Rightarrow 7x + 5y = 46 \quad \text{--- (2)}$$

$$5y = 46 - 7x$$

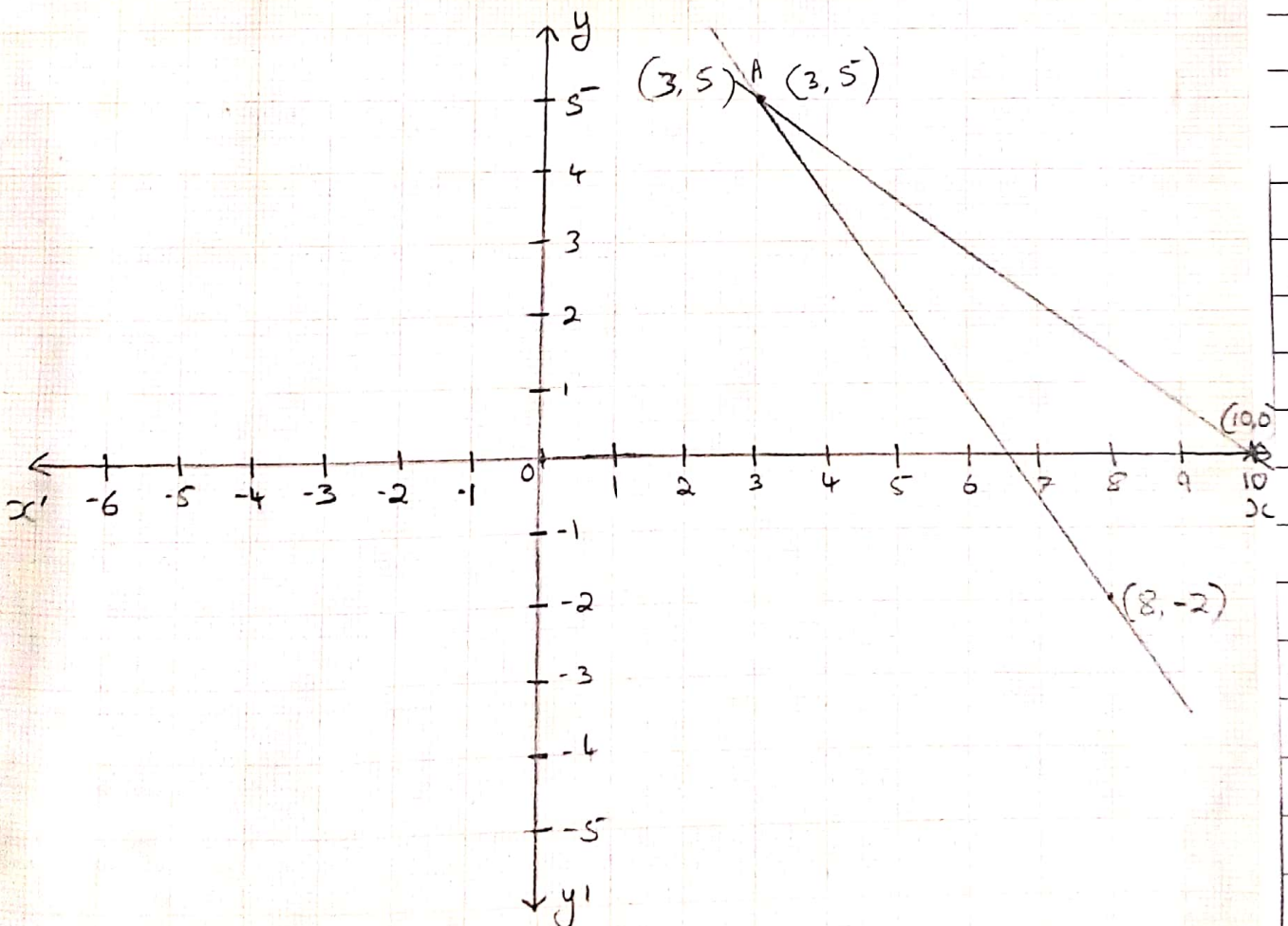
$$y = \frac{46 - 7x}{5}$$

x	3	8
y	5	-2

$$y = \frac{46 - (7 \times 3)}{5} = \frac{46 - 21}{5}$$

$$y = \frac{25}{5} = 5$$

$$y = \frac{46 - 7x}{5} = \frac{46 - 7(8)}{5} = \frac{46 - 56}{5} = \frac{-10}{5} = -2$$



Two lines meet at A (3, 5)

Cost of one pencil = 3

Cost of one pen = 2

2. On comparing the ratios $\frac{a_1}{a_2}$, $\frac{b_1}{b_2}$ and $\frac{c_1}{c_2}$, find out whether the lines representing the following pairs of linear equations intersect at a point, are parallel or coincide.

i) $5x - 4y + 8 = 0$

$7x + 6y - 9 = 0$

$$\frac{a_1}{a_2} = \frac{5}{7}$$

$$\frac{b_1}{b_2} = \frac{-4}{6} = \frac{-2}{3}$$

$$\frac{c_1}{c_2} = \frac{8}{-9}$$

$\Rightarrow \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$ Intersecting lines.

iii) $6x - 3y + 10 = 0$

$2x - y + 9 = 0$

$$\frac{a_1}{a_2} = \frac{6}{2} = 3$$

$$\frac{b_1}{b_2} = \frac{-3}{-1} = 3$$

$$\frac{c_1}{c_2} = \frac{10}{9}$$

$\Rightarrow \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ parallel lines.

ii) $9x + 3y + 12 = 0$

$18x + 6y + 24 = 0$

$$\frac{a_1}{a_2} = \frac{9}{18} = \frac{1}{2}$$

$$\frac{b_1}{b_2} = \frac{3}{6} = \frac{1}{2}$$

$$\frac{c_1}{c_2} = \frac{12}{24} = \frac{1}{2}$$

$\Rightarrow \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$ Co incident lines

3. On comparing ratios $\frac{a_1}{a_2}$, $\frac{b_1}{b_2}$ and $\frac{c_1}{c_2}$, find out whether the following pair of linear equations are consistent, or inconsistent.

iii) $\frac{3}{2}x + \frac{5}{2}y = 7$: $9x - 10y = 14$

$$\frac{a_1}{a_2} = \frac{\frac{3}{2}}{\frac{9}{2}} = \frac{3}{9} = \frac{1}{3}$$

$$\frac{b_1}{b_2} = \frac{\frac{5}{2}}{-10} = \frac{5}{-20} = -\frac{1}{4}$$

$$\frac{c_1}{c_2} = \frac{7}{14} = \frac{1}{2}$$

$$\Rightarrow \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

Intersecting lines
(consistent)

iv) $5x - 3y = 11 : -10x + 6y = -22$

$$\frac{a_1}{a_2} = \frac{5}{-10} = -\frac{1}{2}, \quad \frac{b_1}{b_2} = \frac{-3}{6} = -\frac{1}{2}, \quad \frac{c_1}{c_2} = \frac{11}{-22} = -\frac{1}{2}$$

$$\Rightarrow \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2} \quad \text{Co incident lines (consistent)}$$

v) $\frac{4}{3}x + 2y = 8 : 2x + 3y = 12$

$$\frac{a_1}{a_2} = \frac{\frac{4}{3}}{2} = \frac{4}{3} \times \frac{1}{2} = \frac{2}{3}, \quad \frac{b_1}{b_2} = \frac{2}{3}, \quad \frac{c_1}{c_2} = \frac{8}{12} = \frac{2}{3}$$

$$\Rightarrow \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2} \quad \text{Co incident lines (consistent)}$$

4. Which of the following pairs of linear equations are ~~consistent~~ consistent/inconsistent? If consistent, obtain the solution graphically.

i) $x + y = 5$

$2x + 2y = 10$

$$\frac{a_1}{a_2} = \frac{1}{2}, \quad \frac{b_1}{b_2} = \frac{1}{2}, \quad \frac{c_1}{c_2} = \frac{5}{10} = \frac{1}{2} \quad \text{[consistent]}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

Algebraical eq ① $x + y = 5$

Case I $\therefore -x = 5 - y \leftarrow \boxed{y = 1}$

$x = 5 - 1$

Case II

$x = 4$

$x = 5 - 2 \leftarrow \boxed{y = 2}$

x	4	3
y	1	2

Algebraical eq ② $2x + 2y = 10$

$\boxed{y = 1}$

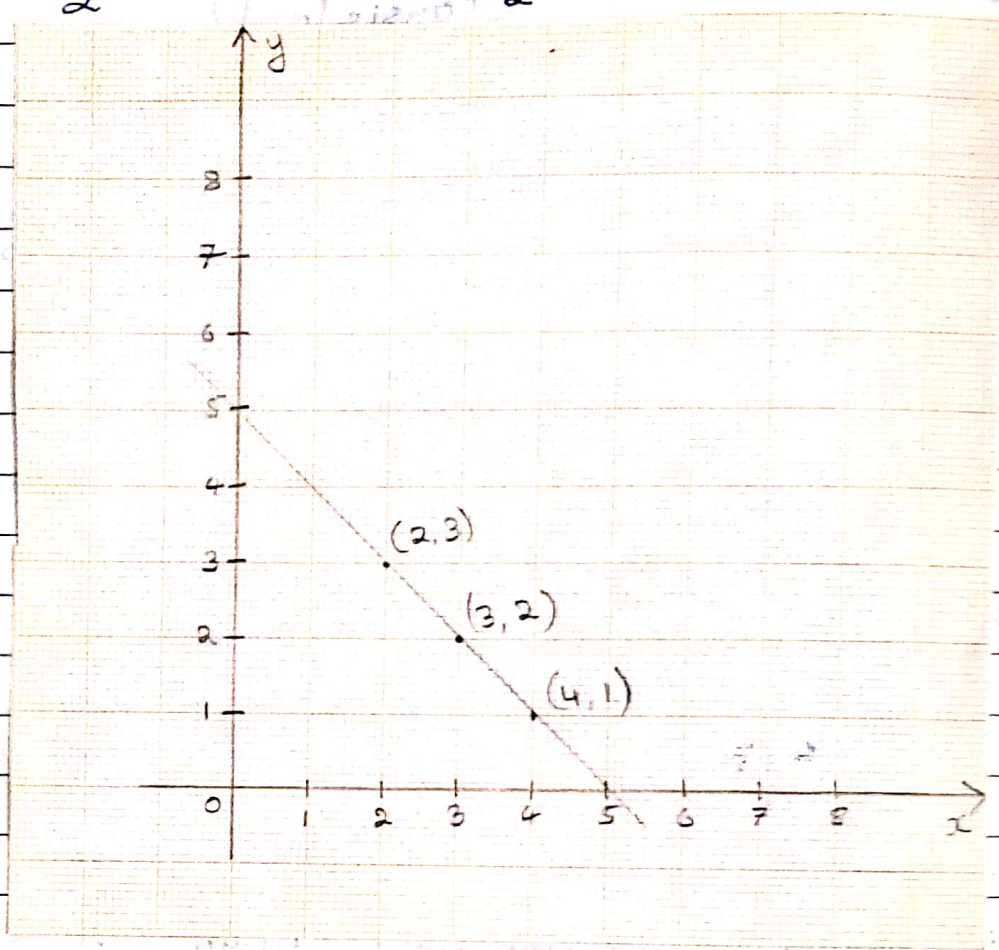
$x = \frac{10 - 2(1)}{2} = \frac{10 - 2}{2}$

$x = 4$

x	4	3
y	1	2

$$\boxed{y=2}$$

$$1) \quad x = \frac{10-2y}{2} = \frac{10-2(2)}{2} = \frac{10-4}{2} = \underline{\underline{3}}$$



$$b) \quad x - y = 8 \quad 3x - 3y = 16$$

$$\frac{a_1}{a_2} = \frac{1}{3} \quad \frac{b_1}{b_2} = \frac{1}{3} \quad \frac{c_1}{c_2} = \frac{8}{16} = \frac{1}{2}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2} \quad \text{inconsistent}$$

$$c) \quad 2x + y - 6 = 0 \quad 4x - 2y - 4 = 0$$

$$\frac{a_1}{a_2} = \frac{2}{4} = \frac{1}{2} \quad \frac{b_1}{b_2} = \frac{1}{-2} = -\frac{1}{2} \quad \frac{c_1}{c_2} = \frac{-6}{-4} = \frac{3}{2}$$

$$\frac{a_1}{a_2} \neq \frac{b_1}{b_2} \neq \frac{c_1}{c_2} \quad \text{Consistent}$$

Algebraical eq. ① $2x + y = 6$

$$2x = 6 - y$$

$$x = \frac{6-y}{2}$$

Case I

$$x = \frac{6-2}{2} = \frac{4}{2} \leftarrow \boxed{y=2}$$

$$x = 2$$

x	2	1
y	2	4

$$x = \frac{6-4}{2} = \frac{2}{2} \quad \boxed{y=4}$$

$$x = 1$$

Algebraical (ii) (a)

$$4x - 2y = 4$$

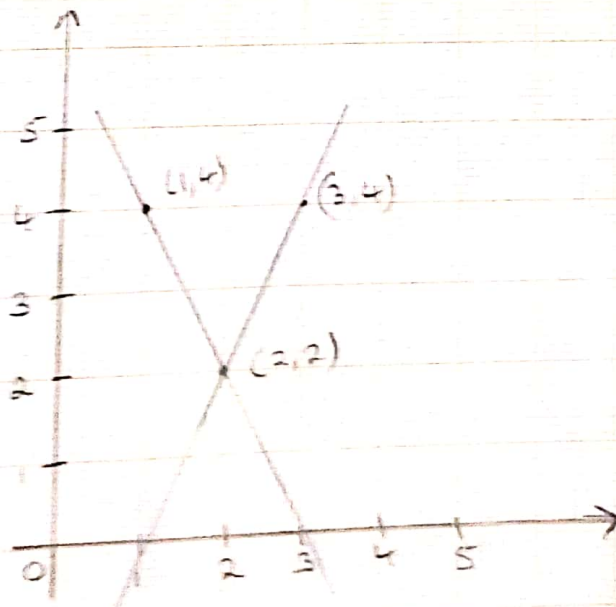
$$4x = 4 + 2y$$

$$x = \frac{4+2y}{4}$$

x	2	3
y	2	4

$$x = \frac{4+2(2)}{4} = \frac{4+4}{4} = \frac{8}{4} = 2 \quad \boxed{y=2}$$

$$x = \frac{4+2(4)}{4} = \frac{4+8}{4} = \frac{12}{4} = 3 \quad \boxed{y=4}$$



2
w
c

iv) $2x - 2y - 2 = 0$ $4x - 4y - 5 = 0$

$\frac{a_1}{a_2} = \frac{2}{4} = \frac{1}{2}$ $\frac{b_1}{b_2} = \frac{-2}{-4} = \frac{1}{2}$ $\frac{c_1}{c_2} = \frac{-2}{-5} \neq \frac{1}{2}$

$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ Inconsistent

5. Half the perimeter of a rectangular garden, whose length is 4m more than its width, is 36m. Find the dimensions of the garden.

Let length be x
Let width be y

Case I

$x = y + 4$ — ①

Case II

$P = 2(x + y)$

$\therefore$ Half of $P = \frac{1}{2} \times 2(x + y)$

$36 = x + y \Rightarrow x + y = 36$

ii) Algebraical eq ①

$x = y + 4$ $(y = 1)$

$x = 1 + 4$

$x = 5$

x	5	6
y	1	2

$x = 2 + 4$ $(y = 2)$

$x = 6$

3. Algebraical eq ②

$x + y = 36$

$x = 36 - y$

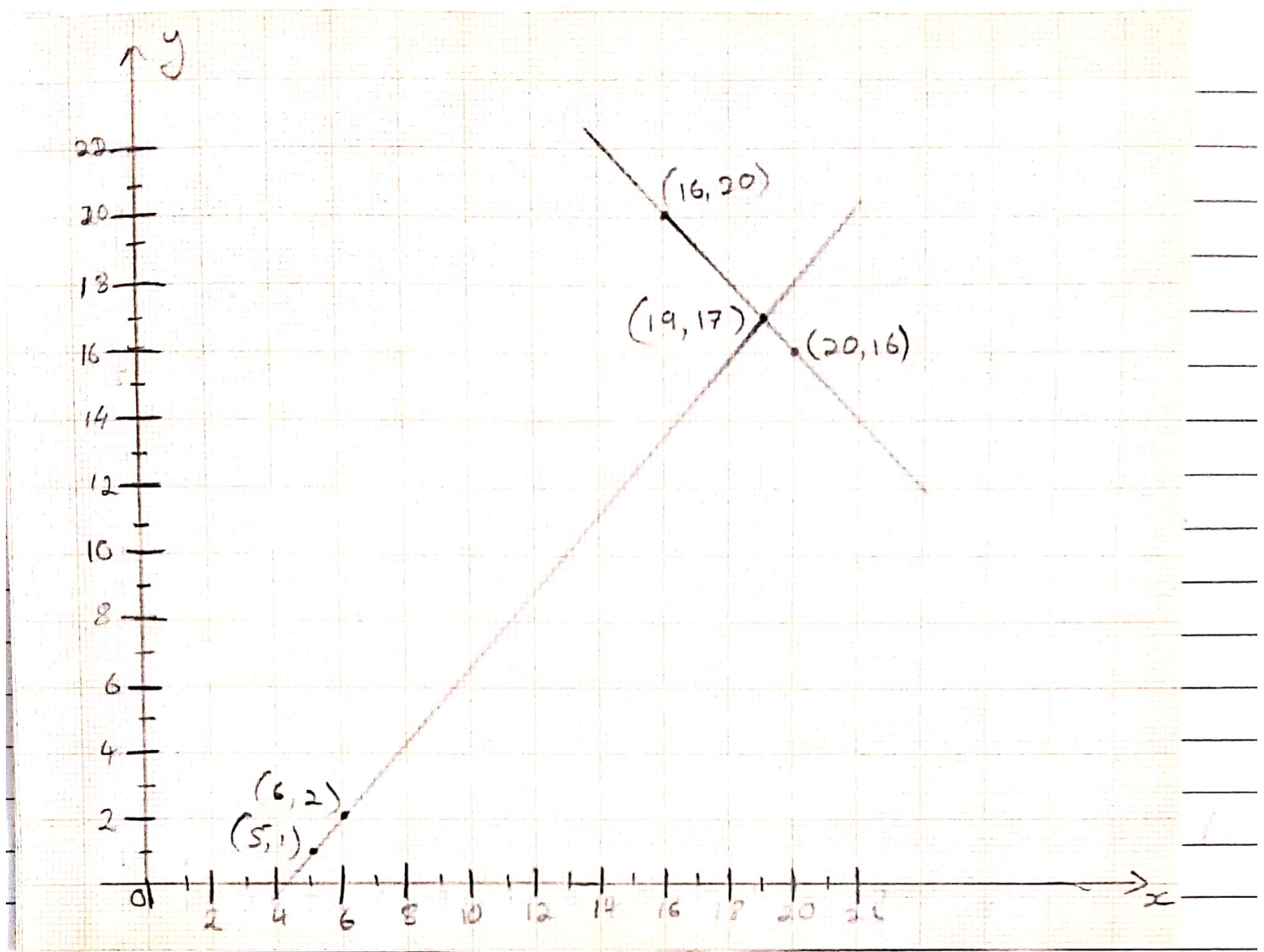
$x = 36 - 20$

$x = 16$

x	16	20
y	20	16

$x = 36 - 16$ $(y = 16)$

$x = 20$



$$x = 19$$

$$y = 17$$

6) Given the linear equations $2x + 3y - 8 = 0$, write another linear equation in two variables such that the geometrical representation of the pair so formed is:

a) intersecting lines

We need $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$

$$2x + 3y = 8$$

$$7x + 7y = 10$$

$$\frac{a_1}{a_2} = \frac{2}{7}$$

$$\frac{b_1}{b_2} = \frac{3}{7}$$

$$\therefore \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$$

$\therefore$ They are intersecting lines

b) parallel lines

we need $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$

$$2x + 3y - 8 = 0$$

$$4x + 6y - 10 = 0$$

$$\frac{a_1}{a_2} = \frac{2}{4} = \frac{1}{2}$$

$$\frac{b_1}{b_2} = \frac{3}{6} = \frac{1}{2}$$

$$\frac{c_1}{c_2} = \frac{-8}{-10} = \frac{4}{5}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

$\therefore$ They are parallel lines.

c) Coincident lines

we need $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$

$$2x + 3y = 8$$

$$4x + 6y = 16$$

$$P_1: x = 1$$

$$P_2: y = 0$$

$$\frac{a_1}{a_2} = \frac{2}{4} = \frac{1}{2}$$

$$\frac{b_1}{b_2} = \frac{3}{6} = \frac{1}{2}$$

$$\frac{c_1}{c_2} = \frac{8}{16} = \frac{1}{2}$$

$$\therefore \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$$

$\therefore$ They are coincident lines.

Q7. Draw the graphs of the equations $x - y + 1 = 0$ and $3x + 2y - 12 = 0$. Determine the coordinates of the vertices of the triangle formed by these lines and the x -axis, and shade the triangular region.

$$x - y + 1 = 0$$

$$x - y = -1$$

$$x = y - 1$$

$$x = 0 - 1$$

$$x = -1$$

$$y = 0$$

$$x = 1 - 1$$

$$x = 0$$

x	-1	0
y	0	1

$$y = 1$$

$$3x + 2y - 12 = 0$$

$$3x = 12 - 2y$$

$$x = \frac{12 - 2y}{3}$$

$$x = \frac{12 - 2(0)}{3}$$

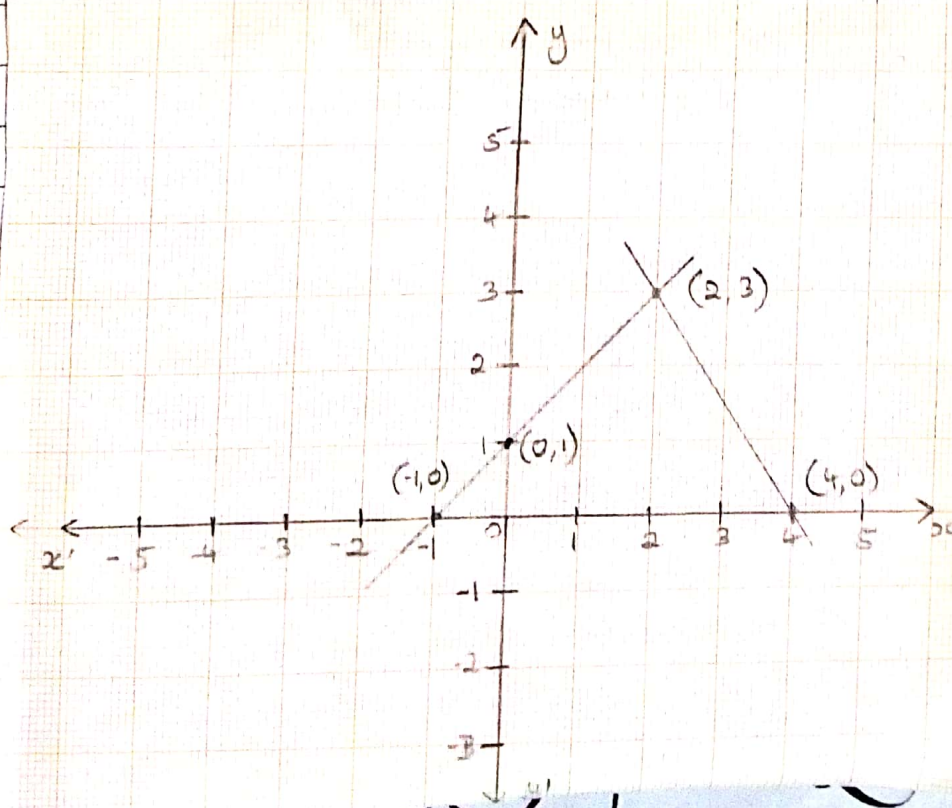
$$x = \frac{12}{3} = 4$$

$$y = 0$$

x	4	2
y	0	3

$$x = \frac{12 - 2(3)}{3}$$

$$= x = \frac{12 - 6}{3} = \frac{6}{3} = 2$$



Vertices of the triangle are $(2, 3)$, $(-1, 0)$ and $(0, 4)$

Ex 3.3

Q1. Solve the following pair of linear equation by the substitution method.

i) $x + y = 14$ - (1)

$x - y = 4$ - (2)

From eq (1)

$$x + y = 14$$

$$x = 14 - y$$
 - (3)

put $x = 14 - y$ in (2)

$$x - y = 4$$

$$(14 - y) - y = 4$$

$$14 - y - y = 4$$

$$14 - 2y = 4$$

$$-2y = 4 - 14$$

$$-2y = -10$$

$$2y = 10$$

$$y = \frac{10}{2}$$

$$y = 5$$

put $y = 5$ in (3)

$$x = 14 - y$$

$$x = 14 - 5$$

$$x = 9$$

$\therefore$ solution are $x = 9$, $y = 5$

ii) $s - t = 3$ - (1)

$\frac{s}{3} + \frac{t}{2} = 6$ - (2)

From eq (1)

$$s - t = 3$$

$$s = 3 + t$$
 - (3)

put (3) in (2)

$$3 + \frac{t}{3} + \frac{t}{2} = 6$$

$$\frac{6 + 2t + 3t}{6} = 6 \quad \text{LCM} = 6$$

$$\frac{6 + 5t}{6} = 6$$

$$6 + 5t = 6 \times 6 = 36$$

$$6 + 5t = 36$$

$$5t = 36 - 6$$

$$5t = 30$$

$$t = \frac{30}{5} = 6$$

put $t = 6$ in (3)

$$s = 3 + t$$

$$s = 3 + 6$$

$$s = 9$$

$\therefore$ solution are $s = 9$, $t = 6$
~~LCM = 6~~

$$3x - y = 3 \quad \text{--- (1)}$$

$$9x - 3y = 9 \quad \text{--- (2)}$$

$$(9x - 3y = 9) \div 3 = 3x - y = 3 \quad \text{--- (2)}$$

Infinitely many solutions ~~coincident~~

$$0.2x + 0.3y = 1.3$$

$$0.4x + 0.5y = 2.3$$

$$(0.2x + 0.3y = 1.3) \times 10 = 2x + 3y = 13 \quad \text{--- (1)}$$

$$(0.4x + 0.5y = 2.3) \times 10 = 4x + 5y = 23 \quad \text{--- (2)}$$

From eq (1)

$$2x + 3y = 13$$

$$2x = 13 - 3y$$

$$x = \frac{13 - 3y}{2} \quad \text{--- (3)}$$

Put (3) in (2)

$$4x + 5y = 23$$

$$4\left(\frac{13 - 3y}{2}\right) + 5y = 23$$

$$2(13 - 3y) + 5y = 23$$

$$26 - 6y + 5y = 23$$

$$26 - y = 23$$

$$-y = 23 - 26$$

$$-y = -3$$

$$y = 3$$

put $y = 3$ in (1)

$$2x + 3(3) = 13$$

$$2x + 9 = 13$$

$$2x = 13 - 9$$

$$2x = 4$$

$$x = \frac{4}{2}$$

$$x = 2$$

$\therefore$ solution are $x = 2$ $y = 3$

$$\sqrt{2}x + \sqrt{3}y = 0 \quad \text{--- (1)}$$

$$\sqrt{3}x - \sqrt{8}y = 0 \quad \text{--- (2)}$$

From eq (1)

$$\sqrt{2}x + \sqrt{3}y = 0$$

$$\sqrt{2}x = -\sqrt{3}y$$

$$\sqrt{2}x = -\sqrt{3}y$$

$$x = \frac{-\sqrt{3}y}{\sqrt{2}} \quad \text{--- (3)}$$

Put (3) in (2)

$$\sqrt{3}x - \sqrt{8}y = 0$$

$$\sqrt{3}\left(\frac{-\sqrt{3}y}{\sqrt{2}}\right) - \sqrt{8}y = 0$$

$$\frac{-3y}{\sqrt{2}} - \sqrt{8}y = 0$$

$$\text{LCM} = \sqrt{2}$$

$$\frac{-3y}{\sqrt{2}} - \sqrt{16}y = 0$$

$$\frac{-3y}{\sqrt{2}} - \frac{4y}{\sqrt{2}} = 0$$

$$\frac{-7y}{\sqrt{2}} = 0$$

$$-7y = 0$$

$$y = \frac{0}{-7}$$

$$y = 0$$

Put $y=0$ in ①

$$\sqrt{2}x + \sqrt{3}y = 0$$

$$\sqrt{2}x + \sqrt{3}(0) = 0$$

$$\sqrt{2}x + 0 = 0$$

$$x = \frac{0}{\sqrt{2}}$$

$$\underline{x = 0}$$

$\therefore$ solutions are $x=0$, $y=0$.

vi) $\frac{3x}{2} - \frac{5y}{3} = -2$

$$\frac{x}{3} + \frac{y}{2} = \frac{13}{6}$$

$$\frac{3x}{2} - \frac{5y}{3} = -2 \quad \text{LCM}=6 \quad \Rightarrow \quad \frac{9x - 10y}{6} = -2$$

$$9x - 10y = -12 \quad \text{--- ①}$$

$$\frac{x}{3} + \frac{y}{2} = \frac{13}{6} \quad \text{LCM}=6 \quad \Rightarrow \quad \frac{2x + 3y}{6} = \frac{13}{6}$$

$$2x + 3y = 13 \quad \text{--- ②}$$

From eq ①

$$9x - 10y = -12$$

$$9x = -12 + 10y$$

$$x = \frac{-12 + 10y}{9} \quad \text{--- ③}$$

Put ③ in ②

$$2x + 3y = 13$$

$$2\left(\frac{-12 + 10y}{9}\right) + 3y = 13$$

$$\frac{-24 + 20y}{9} + 3y = 13 \quad \text{LCM}=9$$

$$\frac{-24 + 20y + 27y}{9} = 13$$

$$\frac{-24 + 47y}{9} = 13$$

$$-24 + 47y = 13 \times 9$$

$$-24 + 47y = 117$$

$$47y = 117 + 24$$

$$47y = 141$$

$$y = \frac{141}{47}$$

$$\underline{y = 3}$$

put $y=3$ in ①

$$9x - 10y = -12$$

$$9x - 10(3) = -12$$

$$9x + 30 = -12$$

$$9x = -12 + 30$$

$$9x = 18$$

$$x = \frac{18}{9}$$

$$x = 2$$

$\therefore$ Solution are $x = 2$ $y = 3$

2. Solve $2x + 3y = 11$ and $2x - 4y = -24$ and hence find the value of 'm' for which $y = mx + 3$

$$2x + 3y = 11 \quad \text{--- (1)}$$

$$2x - 4y = -24 \quad \text{--- (2)}$$

From eq. (1)

$$2x + 3y = 11$$

$$2x = 11 - 3y$$

$$x = \frac{11 - 3y}{2} \quad \text{--- (3)}$$

Put (3) in (2)

$$2x - 4y = -24$$

$$2\left(\frac{11 - 3y}{2}\right) - 4y = -24$$

$$11 - 3y - 4y = -24$$

$$11 - 7y = -24$$

$$-7y = -24 - 11$$

$$-7y = -35$$

$$y = \frac{-35}{-7}$$

$$y = 5$$

Put $y = 5$ in (1)

$$2x + 3y = 11$$

$$2x + 3(5) = 11$$

$$2x + 15 = 11$$

$$2x = 11 - 15$$

$$2x = -4$$

$$x = \frac{-4}{2} = -2$$

$$y = 5 \text{ and } x = -2$$

put $y = 5$ and $x = -2$

$$\text{in } y = mx + 3$$

$$5 = -2m + 3$$

$$5 - 3 = -2m$$

$$2 = -2m$$

$$\therefore m = \frac{-2}{2}$$

$$m = -1$$

Ans: $m = -1$

3) From the pair of linear equations from the following problems and find their solution by substituting method.

i) The difference between two numbers is 26 and one number is three times the other. Find them.

Let the numbers be x and y

Case I : $x - y = 26$ - (1)

Case II : $x = 3y$ - (2)

put (2) in (1)

$$x - y = 26$$

$$3y - y = 26$$

$$2y = 26$$

$$y = \frac{26}{2}$$

$$y = 13$$

Put $y = 13$ in (2)

$$x = 3y$$

$$x = 3 \times 13$$

$$x = 39$$

ii) The larger of two supplementary angles exceeds the smaller by 18 degree. Find them.

Let the larger angle be x

smaller angle be y

Case I

$$x + y = 180^\circ \text{ - (1) (supplementary angles)}$$

Case II

Larger angle exceeds smaller angle by 18°

$$x = y + 18 \text{ - (2)}$$

Put ③ in ①

$$x + y = 180^\circ$$

$$(y + 18) + y = 180$$

$$2y + 18 = 180$$

$$2y = 180 - 18$$

$$2y = 162$$

$$y = \frac{162}{2} = 81$$

Put $y = 81$ in ③

$$x = y + 18$$

$$x = 81 + 18$$

$$x = 99^\circ$$

∴ The larger angle is 99° and the smaller angle is 81°

iii) The coach of a cricket team buys 7 bats and 6 balls for ₹3800. Later, she buys 3 bats and 5 balls for ₹1750. Find the cost of each bat and each ball.

Let the cost of one bat = ₹ x
cost of one ball = ₹ y

Case I

$$7x + 6y = 3800 \quad \text{--- (1)}$$

Case II

$$3x + 5y = 1750 \quad \text{--- (2)}$$

$$3x = \frac{1750 - 5y}{3} \quad \text{--- (2)}$$

put ② in ①

$$7x + 6y = 3800$$

$$7\left(\frac{1750 - 5y}{3}\right) + 6y = 3800$$

$$\frac{12250 - 35y}{3} + \frac{18y}{3} = 3800$$

$$\frac{12250 + 13y}{3} = 3800$$

$$12250 + 13y = 3800 \times 3$$

$$13y = 3800 \times 3 - 12250$$

$$\frac{13y}{13} = \frac{-8450}{13}$$

iv) The taxi charge in a city consist of a fixed charge together with the charge for the distance covered. For distance of 10 km, the charge paid is ₹105 and for a journey of 15 km, the charge paid is ₹155. What are the fixed charge and the charge per km? How much does a person have to pay for travelling a distance of 25 km?

Let fixed charge be Rs x

Charge per km = Rs y

Case I: $x + 10y = 105$ - (1)

Case II: $x + 15y = 155$ - (2)

From (1)

$$x + 10y = 105$$

$$x = 105 - 10y \quad - (3)$$

Put (3) in (2)

$$x + 15y = 155$$

$$105 - 10y + 15y = 155$$

$$105 + 5y = 155$$

$$5y = 155 - 105$$

$$5y = 50$$

$$y = \frac{50}{5} = 10$$

Put $y = 10$ in (3)

$$x = 105 - 10y$$

$$x = 105 - 10(10)$$

$$x = 105 - 100$$

$$x = 5$$

$\therefore$ The fixed charges are ₹5 and charge per km is ₹10

Charge for a distance of 25 km = $x + 25y$
 $= 5 + 25(10)$

$$= 5 + 250 = \underline{\underline{255}}$$

* Q) A fraction becomes $\frac{9}{11}$, if 2 is added to both the numerator and the denominator. If 3 is added to both the numerator and denominator it becomes $\frac{5}{6}$. Find the fraction.

Let the fraction be $\frac{x}{y}$

Case I $\frac{x+2}{y+2} = \frac{9}{11}$ cross multiply

$$11(x+2) = 9(y+2)$$

$$11x + 22 = 9y + 18$$

$$11x - 9y = 18 - 22$$

$$11x - 9y = -4 \quad \text{--- (1)}$$

Case II $\frac{x+3}{y+3} = \frac{5}{6}$ cross multiply

$$6(x+3) = 5(y+3)$$

$$6x + 18 = 5y + 15$$

$$6x - 5y = 15 - 18$$

$$6x - 5y = -3 \quad \text{--- (2)}$$

Ex 3.4

1. Solve the following pair of linear equations by the eliminating method and substitution method.

ii) $3x + 4y = 10$ and $2x - 2y = 2$

$$3x + 4y = 10 \quad \text{--- ①}$$

$$2x - 2y = 2 \quad \text{--- ②} \quad \times 2$$

$$\begin{array}{r} 3x + 4y = 10 \\ + \quad 4x - 4y = 4 \\ \hline \end{array}$$

$$7x = 14$$

$$x = 2$$

$$x = 2$$

Put $x = 2$ in eq ①

$$3x + 4y = 10$$

$$3(2) + 4y = 10$$

$$6 + 4y = 10$$

$$4y = 10 - 6$$

$$y = \frac{4}{4}$$

$$\underline{\underline{y = 1}}$$

iv) $\frac{x}{2} + \frac{2y}{3} = -1$

and $x - \frac{y}{3} = 3$

$$\frac{x}{2} + \frac{2y}{3} = -1 \quad \text{--- ①}$$

$$x - \frac{y}{3} = 3 \quad \text{--- ②} \quad \times 2$$

$$\frac{x}{2} + \frac{2y}{3} = -1$$

$$+ \quad 2x - \frac{2y}{3} = 6$$

$$\frac{x}{2} + 2x = 5$$

LCM = 2

$$\frac{x + 4x}{2} = 5$$

$$\frac{8x}{2} = 8$$

$$\frac{x}{2} = 1$$

$$x = 2$$

put $x=2$ in eq ①

$$\frac{x}{2} + \frac{2y}{3} = -1$$

$$1 + 2y = -3$$

$$2y = -3 - 1$$

$$y = \frac{-4}{2}$$

$$y = -2$$

i) $x+y=5$ and $2x-3y=4$

$$x+y=5 \quad \text{--- ①} \quad (\times 3)$$

$$2x-3y=4$$

$$3x+3y=15$$

$$2x-3y=4$$

$$5x=19$$

$$x = \frac{19}{5}$$

put $x = \frac{19}{5}$ in eq ①

$$x+y=5$$

$$\frac{19}{5} + y = 5$$

$$19 + 5y = 25$$

$$19 + 5y = 25$$

$$5y = 25 - 19$$

$$5y = 6$$

$$y = \frac{6}{5}$$

$$y = \frac{6}{5}$$

2. Form the pair of linear equations in the following problems, and find their solution by the eliminating method:

i) If we add 1 to the numerator and subtract 1 from the denominator, a fraction reduces to 1. It becomes $\frac{1}{2}$ if we only add 1 to the denominator. What is the fraction?

Let the fraction be $\frac{x}{y}$

Case I $\frac{x+1}{y-1} = 1$

$$x+1 = y-1$$

$$x-y = -1-1$$

$$x-y = -2 \quad \text{--- (1)}$$

Case II $\frac{x}{y+1} = \frac{1}{2}$

$$2x = y+1$$

$$2x-y = 1 \quad \text{--- (2)}$$

$$x-y = -2 \quad \text{--- (1)}$$

$$2x-y = 1 \quad \text{--- (2) } \times -1$$

$$x-y = -2$$

$$-2x+y = 1$$

$$-x = -3$$

$$x = 3$$

put $x=3$ in eq (1)

$$3-y = -2$$

$$-y = -2-3$$

$$-y = -5$$

$$y = 5$$

Fraction is $\frac{3}{5}$

ii) Five years ago, Nuri was thrice as old as Sonu. Ten years later, Nuri will be twice as old as Sonu. How old are Nuri and Sonu?

Let Nuri present age = x years

Sonu present age = y years

Case I (5 years ago)

Nuri age = $(x-5)$ years

Sonu age = $(y-5)$ years

Nuri age = 3 [Sonu age]

$$x-5 = 3[y-5]$$

$$x-5 = 3y-15$$

$$x-3y = -15+5$$

$$x-3y = -10 \quad \text{--- (1)}$$

Case II (10 years later)

Nuri age = $(x+10)$ years

Sonu age = $(y+10)$ years

$$x+10 = 2(y+10)$$

$$x+10 = 2y+20$$

$$x-2y = 20-10$$

$$x-2y = 10 \quad \text{--- (2)}$$

$$x-3y = -10 \quad \text{--- (1)}$$

$$x-2y = 10 \quad \text{--- (2) } \times -1$$

$$x-3y = -10$$

$$x-2y = 10$$

$$-y = -20$$

$$y = 20$$

Put $y=20$ in eq (1)

$$x-3(20) = -10$$

$$x-60 = -10$$

$$x = -10+60$$

$$x = 50$$

Nuri age = 50

Sonu age = 20

iii) The sum of the digits of a two-digit number is 9. Also, nine times this number is twice the number obtained by reversing the order of the digits. Find the numbers.

Let unit digit be y

Ten's digit be x

$$\text{number} = (y \times 1) + (x \times 10) = y + 10x$$

New number after interchanging the digits

$$\text{unit digit} = x$$

$$\text{Ten's digit} = y$$

$$\text{New no} = (x \times 1) + (y \times 10)$$

$$= x + 10y$$

Case I $x + y = 9$ - (1)

Case II $9(\text{no}) = 2(\text{new number})$

$$9(y + 10x) = 2(x + 10y)$$

$$9y + 90x = 2x + 20y$$

$$90x - 2x = 20y - 9y$$

$$88x = 11y$$

$$88x - 11y = 0 \quad \left[\div 11 \right]$$

$$8x - y = 0 \quad \text{--- (2)}$$

$$x + y = 9$$

$$8x - y = 0$$

$$9x = 9$$

$$x = 9/9$$

$$x = 1$$

put $x=1$ in eq (1)

$$x + y = 9$$

$$1 + y = 9$$

$$y = 9 - 1$$

$$y = 8$$

$$\begin{aligned} \text{No} &= y + 10x \\ &= 8 + 10(1) \\ &= 8 + 10 \\ &= 18 \end{aligned}$$

Q) Meena went to a bank to withdraw ₹ 2000. She asked the cashier to give her ₹ 50 and ₹ 100 notes only. Meena got 25 notes in all. Find how many notes of ₹ 50 and ₹ 100 did she receive.

Let the number of Rs 50 notes = x
 number of Rs 100 notes = y
 Total number of notes she received = 25

Case I $x + y = 25$ - ①

Case II $50x + 100y = 2000$ $[\div 50]$
 $x + 2y = 40$ - ②

$x + y = 25$ - ①

$x + 2y = 40$ - ② $\times -1$

$$\begin{array}{r} x + y = 25 \\ -x - 2y = -40 \\ \hline 3y = 65 \\ y = 15 \end{array}$$

put $y = 15$ in eq ①

$x + y = 25$

$x + 15 = 25$

$x = 25 - 15$

$x = 10$

number of Rs 50 notes = 10

number of Rs 100 notes = 15

Ex 3.5

2.1) For which value of a and b does the following pair of linear equations have an infinite no. of solution?

$$2x + 3y = 7$$

$$(a-b)x + (a+b)y = 3a+b-2$$

$$\frac{a_1}{a_2} = \frac{2}{a-b}, \quad \frac{b_1}{b_2} = \frac{3}{a+b}, \quad \frac{c_1}{c_2} = \frac{7}{3a+b-2}$$

$$\frac{2}{a-b} = \frac{3}{a+b} = \frac{7}{3a+b-2}$$

$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$ then infinite many solutions when in this case

$$\Rightarrow \frac{2}{a-b} \neq \frac{3}{a+b}$$

$$2(a+b) = 3(a-b)$$

$$2a + 2b = 3a - 3b$$

$$2a + 2b - 3a + 3b = 0$$

$$-a + 5b = 0 \quad \text{--- (1)}$$

$$\Rightarrow \frac{3}{a+b} \neq \frac{7}{3a+b-2}$$

$$3(3a+b-2) = 7(a+b)$$

$$9a + 3b - 6 = 7a + 7b$$

$$9a + 3b - 6 - 7a - 7b = 0$$

$$2a - 4b = 6 \quad (\div 2)$$

$$a - 2b = 3 \quad \text{--- (2)}$$

$$-a + 5b = 0 \quad \text{--- (1)}$$

$$a - 2b = 3 \quad \text{--- (2)}$$

$$3b = 3$$

$$b = \frac{3}{3}$$

$$\underline{b = 1}$$

put $b=1$ in eq. (1)

$$a - 2b = 3$$

$$a - 2(1) = 3$$

$$a - 2 = 3$$

$$a = 3 + 2$$

$$\underline{a = 5}$$

ii) For which value of k will the following pair of linear equations have no solution?

$$3x + y = 1$$

$$(2k-1)x + (k-1)y = 2k+1$$

$$\frac{a_1}{a_2} = \frac{3}{2k-1}, \quad \frac{b_1}{b_2} = \frac{1}{k-1}, \quad \frac{c_1}{c_2} = \frac{1}{2k+1}$$

$$\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2} \quad [\text{no solutions}]$$

$$\frac{3}{2k-1} = \frac{1}{k-1} \neq \frac{1}{2k+1}$$

$$\Rightarrow \frac{3}{2k-1} \neq \frac{1}{k-1}$$

$$3(k-1) = 1(2k-1)$$

$$3k - 3 = 2k - 1$$

$$3k - 2k = -1 + 3$$

$$\underline{k = 2}$$

3. Solve the following pair of linear equations by the substitution and cross multiplication method.

$$8x + 5y = 9 \quad - (1) \quad (\times 2)$$

$$8x + 2y = 4 \quad - (2) \quad (\times 5)$$

$$16x + 10y = 18$$

$$-15x + 10y = -20$$

$$x = -2$$

put $x = -2$ in eq (1)

$$8(-2) + 5y = 9$$

$$-16 + 5y = 9$$

$$5y = 9 + 16$$

$$5y = 25$$

$$y = \frac{25}{5}$$

$$y = 5$$

$$\therefore \underline{x = -2 \text{ and } y = 5}$$

4. Form the pair of linear equations in the following problems and find their solutions by an algebraical method.

i) A part of monthly hostel charge is fixed and the remaining depends on the number of days one has taken food in the mess. When a student A takes food for 20 days she has to pay 2000 as hostel charges where as student B, who takes food for 26 days, pays 2180 as hostel charge. Find the ^{fixed} charges and the cost of food per day.

Let fixed charges = Rs x
Cost of food/day = Rs y

Case I (20 days $\rightarrow$ Rs 1000)

$$x + 20y = 1000 \quad \text{--- (1)}$$

Case II (26 days $\rightarrow$ Rs 1180)

$$x + 26y = 1180 \quad \text{--- (2)}$$

$$x + 20y = 1000 \quad \text{--- (1)}$$

$$x + 26y = 1180 \quad \text{--- (2)}$$

$$\begin{array}{r} x + 20y = 1000 \\ -x + 26y = -1180 \\ \hline \end{array}$$

put $y = 30$ in eq (1)

$$x + 26y = -1180$$

$$y = \frac{-1180}{26}$$

$$y = 30$$

$$x + 20(30) = 1000$$

$$x + 600 = 1000$$

$$x = 1000 - 600$$

$$x = 400$$

ii) A fraction becomes $\frac{1}{3}$ when 1 is subtracted from the numerator and it becomes $\frac{1}{4}$ when 8 is added to the denominator. Find the fraction.
 Let fraction be $\frac{x}{y}$

Case I $\frac{x-1}{y} = \frac{1}{3}$

$$3(x-1) = 1y$$

$$3x - 3 = y$$

$$3x - y = 3 \quad \text{--- (1)}$$

Case II

$$\frac{x}{y+8} = \frac{1}{4}$$

$$4x = 1(y+8)$$

$$4x = y+8$$

$$4x - y = 8 \quad \text{--- (2)}$$

$$3x - y = 3 \quad \text{--- (1)}$$

$$4x - y = 8 \quad \text{--- (2)}$$

put $x = 5$ in eq 1

$$3(5) - y = 3$$

$$15 - y = 3$$

$$-y = 3 - 15$$

$$-y = -12$$

$$y = 12$$

Fraction is $\frac{5}{12}$

iii) Yash scored 40 marks in a test, getting 3 marks for each right answers and losing 1 mark for each wrong answer. He had 4 marks been awarded for each correct answer and 2 marks been deducted for each incorrect answer, Then Yash would have scored 50 marks. How many questions were there in the test?

Let no. of right answers = x
no. of wrong answers = y

Case I $3x - y = 40 \quad \text{--- (1)}$

Case II $4x - 2y = 50 \quad \text{--- (2)}$

$$-6x + 2y = -80 \quad \text{--- (3)}$$

$$4x - 2y = 50 \quad \text{--- (2)}$$

$$-2x = -30$$

$$x = \frac{30}{2}$$

$$x = 15$$

put $x = 15$ in eq (1)

$$3(15) - y = 40$$

$$45 - y = 40$$

$$-y = 40 - 45$$

$$-y = -5$$

$$y = 5$$

No. of right answers = 15

No. of wrong answers = 5

Total no. of questions = 20

iv) Place A and B are 100km apart on a highway. One car starts from A and another from B at the same time. If the cars travel in the same direction at different speeds they meet in 5 hrs. If they travel towards each other, they meet in 1 hour. What are the speeds of the cars?

Let speed of car starting from A = x km/hr
 speed of car starting from B = y km/hr

Case I [Same direction]

time = 5 hrs, distance = 100 km, Speed = $(x-y)$ km/hr

$$\text{speed} = \frac{d}{t}$$

$$x-y = \frac{100}{5}$$

$$x-y = 20 \quad \text{--- (1)}$$

Case II [Oppo. direction]

time = 1 hr, distance = 100 km, Speed = $(x+y)$ km/hr

$$\text{Speed} = \frac{d}{t}$$

$$x+y = \frac{100}{1}$$

$$x+y = 100 \quad \text{--- (2)}$$

$$x-y = 20$$

$$x+y = 100$$

$$2x = 120$$

$$x = \frac{120}{2}$$

$$x = 60$$

put $x = 60$ in eq (2)

$$60+y = 100$$

$$y = 100 - 60$$

$$y = 40$$

Speed of car starting from A = 60 km/hr
 B = 40 km/hr

1) The area of a rectangle gets reduced by 9 square units, if its length is reduced by 5 units and breadth is increased by 3 units. If we increase the length by 3 units and the breadth by 2 units, the area increases by 67 square units. Find the dimensions of the rectangle.

Let length = x

breadth = y

Area = $l \times b$

= xy

Case I (Area reduce by 9) = (length - 5) (Breadth + 3)

$$xy - 9 = (x - 5)(y + 3)$$

$$xy - 9 = x(y + 3) - 5(y + 3)$$

$$xy - 9 = xy + 3x - 5y - 15$$

$$-9 = 3x - 5y - 15$$

$$-9 + 15 = 3x - 5y$$

$$6 = 3x - 5y \quad \text{--- (1)}$$

Case II (A + 67) = (l + 3) (b + 2)

$$xy + 67 = (x + 3)(y + 2)$$

$$xy + 67 = x(y + 2) + 3(y + 2)$$

$$xy + 67 = xy + 2x + 3y + 6$$

$$67 = 2x + 3y + 6$$

$$67 - 6 = 2x + 3y$$

$$61 = 2x + 3y \quad \text{--- (2)}$$

$$3x - 5y = 6 \quad \text{--- (1)} \quad (\times 3)$$

$$2x + 3y = 61 \quad \text{--- (2)} \quad (\times 5)$$

$$9x - 15y = 18$$

$$10x + 15y = 305$$

$$19x = 323$$

$$x = \frac{323}{19} = 17$$

put $x = 17$ in eq (1)

$$6 = 3(17) - 5y$$

$$6 = 51 - 5y$$

$$-51 = -5y \quad -5y = -45 \quad y = 9$$

$\therefore$ length = 17
breadth = 9

Ex 3.6

1. Solve the following pairs of equations by reducing them to a pair of linear equations.

ii) $\frac{2}{\sqrt{x}} + \frac{3}{\sqrt{y}} = 2$ $\frac{4}{\sqrt{x}} - \frac{9}{\sqrt{y}} = -1$ ①

$$\frac{6}{\sqrt{x}} + \frac{9}{\sqrt{y}} = 6$$

$$\frac{4}{\sqrt{x}} - \frac{9}{\sqrt{y}} = -1$$

$$\frac{10}{\sqrt{x}} = 5$$

$$5\sqrt{x} = 10$$

$$\sqrt{x} = \frac{10}{5}$$

$$\sqrt{x} = 2$$

$$(\sqrt{x})^2 = (2)^2$$

$$\underline{x = 4}$$

put $\sqrt{x} = 2$ in eq ①

$$\frac{2}{\sqrt{x}} + \frac{3}{\sqrt{y}} = 2$$

$$\frac{2}{2} + \frac{3}{\sqrt{y}} = 2$$

$$1 + \frac{3}{\sqrt{y}} = 2$$

$$\frac{3}{\sqrt{y}} = 2 - 1$$

$$\frac{3}{\sqrt{y}} = 1$$

$$\sqrt{y} = 3$$

squaring on both sides

$$(\sqrt{y})^2 = 3^2$$

$$\underline{y = 9}$$

$$iv) \frac{5}{x-1} + \frac{1}{y-2} = 2 - ① (\times 3) \quad \frac{6}{x-1} - \frac{3}{y-2} = 1 - ②$$

$$\frac{15}{x-1} + \frac{3}{y-2} = 6$$

$$\frac{6}{x-1} - \frac{3}{y-2} = 1$$

$$\frac{21}{x-1} = \frac{7}{1}$$

$$7(x-1) = 21$$

$$7x - 7 = 21$$

$$7x = 21 + 7$$

$$7x = 28$$

$$\underline{x = 4}$$

put $x = 4$ in eq ②

$$\frac{6}{x-1} - \frac{3}{y-2} = 1$$

$$\frac{6}{4-1} - \frac{3}{y-2} = 1$$

$$\frac{6}{3} - \frac{3}{y-2} = 1$$

$$2 - \frac{3}{y-2} = 1$$

$$\frac{2(y-2) - 3}{(y-2)} = 1$$

$$\frac{2y - 4 - 3}{y-2} = 1$$

$$2y - 7 = y - 2$$

$$2y - y = -2 + 7$$

$$\underline{y = 5}$$

$$v) \frac{7x-2y}{xy} = 5 \quad \text{--- (1)} \quad \times 7$$

$$\frac{8x+7y}{xy} = 15 \quad \text{--- (2)} \quad \times 2$$

$$49x - 14y = 35xy \quad \text{--- (1)}$$

$$16x + 14y = 30xy \quad \text{--- (2)}$$

$$65x = 65xy$$

$$y = 1$$

put $y = 1$ in eq (1)

$$7x - 2y = 5xy$$

$$7x - 2(1) = 5x(1)$$

$$7x - 2 = 5x$$

$$7x - 5x = 2$$

$$2x = 2$$

$$x = 1$$

$$vii) \frac{10}{x+y} + \frac{2}{x-y} = 4 \quad \text{--- (1)} \quad \times 5$$

$$\frac{15}{x+y} + \frac{5}{x-y} = -2 \quad \text{--- (2)} \quad \times 2$$

$$\frac{50}{x+y} + \frac{10}{x-y} = 20 \quad \text{--- (1)}$$

$$\frac{30}{x+y} - \frac{10}{x-y} = -4 \quad \text{--- (2)}$$

$$\frac{80}{x+y} = 16 \quad \text{--- (1)}$$

$$16(x+y) = 80$$

$$x+y = \frac{80}{16}$$

$$x+y = 5 \quad \text{--- (3)}$$

$$x = 5 - y \quad \text{--- (4)}$$

put $x = 5 - y$ in eq ①

$$\frac{10}{5-y+y} + \frac{2}{5-y-y} = 4$$

$$\frac{10^2}{2} + \frac{2}{5-2y} = 4$$

$$2 + \frac{2}{5-2y} = 4$$

$$\frac{2}{5-2y} = 4 - 2$$

$$\frac{2}{5-2y} = \frac{2}{1}$$

$$2(5-2y) = 2 \times 1$$

$$5-2y = 1$$

$$-2y = 1 - 5$$

$$+2y = -4$$

$$\underline{y = 2}$$

put $y = 2$ in eq ③

$$x = 5 - y$$

$$x = 5 - 2$$

$$\underline{x = 3}$$

* 2. Formulate the following problems as pair of equations and hence find their solutions:

i) Ritu can row downstream 20 km in 2 hours, and upstream 4 km in 2 hrs. Find her speed of rowing in still water and the speed of the current.

Let speed of rowing in still water = x km/hr

speed of current = y km/hr

Case I (downstream)

$d = 20$ km, $t = 2$ hrs

Speed = $(x+y)$ km/hr

$$\text{Speed} = \frac{d}{t}$$

$$x+y = \frac{20}{2}$$

$$x+y = 10 \quad \text{--- (1)}$$

Case II (upstream)

$d = 4$ km, $t = 2$ hrs

Speed = $(x-y)$ km/hr

$$\text{Speed} = \frac{d}{t}$$

$$x-y = \frac{4}{2}$$

$$x-y = 2 \quad \text{--- (2)}$$

$$x+y = 10$$

$$x-y = 2$$

$$2x = 12$$

$$x = 6$$

put $x = 6$ in eq (1)

$$x+y = 10$$

$$6+y = 10$$

$$y = 10 - 6$$

$$y = 4$$

Speed of still water = 6 km/hr

Speed of current = 4 km/hr

ii) 2 women and 5 men can together finish an embroidery work in 4 days, while 3 women and 6 men can finish in 3 days. Find the time taken by 1 woman alone to finish the work, and also that taken by 1 man.

Let 1 man finish the work in x days

1 woman finish the work in y days

So, 1 man 1 days work = $\frac{1}{x}$

1 woman 1 days work = $\frac{1}{y}$

Case I [2 women + 5 men = 4 days]

$$2 \times \frac{1}{y} + 5 \times \frac{1}{x} = 4 \text{ days}$$

$$\frac{2}{y} + \frac{5}{x} = 4 \text{ days} \quad - (1) \times 3$$

Case II [3 women + 6 men = 3 days]

$$3 \times \frac{1}{y} + 6 \times \frac{1}{x} = 3 \text{ days}$$

$$\frac{3}{y} + \frac{6}{x} = 3 \text{ days} \quad - (2) \times -2$$

$$\frac{6}{y} + \frac{15}{x} = \frac{3}{4}$$

$$\frac{-6}{y} - \frac{12}{x} = -\frac{2}{3}$$

$$\frac{3}{x} = \frac{3}{4} - \frac{2}{3}$$

$$\frac{3}{x} = \frac{3 \times 3 - 2 \times 4}{12}$$

$$\frac{3}{x} = \frac{9 - 8}{12}$$

$$\frac{3}{x} = \frac{1}{12}$$

$$\underline{x = 36}$$

put $x = 36$ in eq ②

$$\frac{3}{y} + \frac{6}{x} = \frac{1}{3}$$

$$\frac{3}{y} + \frac{6}{36} = \frac{1}{3}$$

$$\frac{3}{y} + \frac{1}{6} = \frac{1}{3}$$

$$\frac{3}{y} = \frac{1}{3} - \frac{1}{6}$$

$$\frac{3}{y} = \frac{2-1}{6}$$

$$\frac{3}{y} = \frac{1}{6}$$

$$\underline{y = 18}$$

time 1 man works = 36 hrs

time 1 man works = 18 hrs

ii) Roohi travels 300km to her home partly by train and partly by bus. She takes 4 hours if she travels 60km by train and the remaining by bus. If she travels 100km by train and the remaining by bus, she takes 10 mins longer. Find the speed of the train and the bus separately.

Let speed of the train = x km/hr

speed of the bus = y km/hr

Total distance she travels = 300km

Case I

$t = 4$ hrs

distance traveled by train = 60km

distance traveled by bus = $300 - 60 = 240$

$t = \frac{\text{distance}}{\text{speed}}$

$$4 = \frac{60}{x} + \frac{240}{y} \quad [\div 4]$$

$$1 = \frac{15}{x} + \frac{60}{y} \quad - (1)$$

Case II

$t = 4 \text{ hrs } 10 \text{ mins} = 4 \left(\frac{10}{60} \right) \text{ hrs} = 4 \frac{1}{6} = \frac{25}{6}$

distance traveled by train = 100km

distance traveled by bus = $300 - 100 = 200$ km

$t = \frac{d}{s}$

$$\frac{25}{6} = \frac{100}{x} + \frac{200}{y} \quad [\div 25]$$

$$\frac{1}{6} = \frac{4}{x} + \frac{8}{y} \quad - (2)$$

$$1 = \frac{15}{x} + \frac{60}{y} \quad - (1) \quad (x \times 4)$$

$$\frac{1}{6} = \frac{4}{x} + \frac{8}{y} \quad - (2) \quad (x \times 15)$$

$$4 = \frac{60}{x} + \frac{240}{y}$$

$$-15 = \frac{-60}{x} + \frac{120}{y}$$

$$4 - 15 = \frac{120}{y}$$

$$\frac{24 - 15}{6} = \frac{120}{y}$$

$$\frac{9}{6} = \frac{120}{y}$$

$$\frac{3}{2} = \frac{120}{y}$$

$$y = 80$$

put $y = 80$ in eq (1)

$$\frac{1}{6} = \frac{4}{x} + \frac{8}{80}$$

$$\frac{1}{6} = \frac{4}{x} + \frac{8}{80}$$

$$\frac{1}{6} = \frac{4}{x} + \frac{1}{10}$$

$$\frac{1}{6} - \frac{1}{10} = \frac{4}{x}$$

$$\frac{10 - 6}{60} = \frac{4}{x}$$

$$\frac{4}{60} = \frac{4}{x}$$

$$x = 60$$

Speed of train = 60 km/hr

Speed of bus = 80 km/hr